

8.3/ $U(r) = -k/r$ so if $k \rightarrow k/2$ U decreases by a factor of 2.

The original orbit is circular so $T = \text{constant}$ and $V = \text{constant}$.

By the virial theorem $\langle T \rangle = -\frac{1}{2} \langle U \rangle$, but, because it is a circular orbit $\langle T \rangle = T$ and $\langle U \rangle = U$, both constants.

\therefore The kinetic energy in the circular orbit is

$$T = -\frac{1}{2}U \text{ where } U \text{ is the original potential energy}$$

The original energy is

$$E_1 = T + U = -\frac{1}{2}U + U = \frac{1}{2}U$$

Now, when $k \rightarrow k/2$ "suddenly" the kinetic energy doesn't change, but $U \rightarrow U/2$.

The new energy is therefore

$$E_2 = -\frac{1}{2}U + \frac{U}{2} = 0$$

The eccentricity is given by

$$e = \sqrt{1 + \frac{2El^2}{\mu k^2}} \rightarrow 1 \text{ for } E=0$$

i.e. a parabolic orbit